

**INTERNATIONAL JOURNAL OF ENGINEERING SCIENCES & RESEARCH
TECHNOLOGY****MODELING, DESIGN & ANALYSIS OF DIFFERENTIAL GEAR BOX AND ITS
HOUSING THROUGH FEM, SOLIDWORK & ANSYS BENCHWORK 14.0****Shashank Pandey^{*1}, Nikhilesh N. Singh² & Dr. Prabhat Kumar Sinha³**^{*1}M. Tech. Scholar, Dept. of Mechanical Engineering, SHUATS, Allahabad, U.P., India^{2&3}Assistant Professor, Dept. of Mechanical Engineering, SHUATS Allahabad, U.P., India

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ABSTRACT

In this paper the differential gears assembly and its housing are analyzed for the vibrational effect on a system in which the life of the gears is determined within different frequency range in the platform of Ansys-14.0 with use of solidworks modeling. In this type of analysis the gear housing is also effected by vibration in casing that surrounds the gear box. The main objective of gear is to protect and to provide a safe platform to get good gear transmission. It is also gives a supports for moving parts and protected it from outside condition. The differential couples and the propeller shaft on the pinion, which is runs on the ring gear or crown gear of the differential & it is also helps as the reduction in gearing friction. And enhance the life of the gear. Hence will subjected to vibration so it becomes compalsary to calculate the response of differential gear housing in different vibration conditions and it is also finding there natural frequencies. This can be most important tool in designing the differential gear housing free from fatigue failures caused by the resonance. The design of the gear housing should be appropriate a methodology for allocated with factors causing vibrations and to promote scientific means and to minimize the effects of frequencies. This vibration analysis is done by using ANSYS 14.0 software as a computational technique and validation and the modeling of differential gear box is done by using of SOLIDWORKS.

KEYWORDS: differential gears, natural frequency, Ansys 14.0.**I. INTRODUCTION**

In automobiles and other wheeled vehicles, the differential permit the outer drive wheel for rotating faster than the inner drive wheel on the time of a turn. This is must when the vehicle makes a turn, making the wheel when that is traveling around the outside of the turning curve roll farther and faster than the other. The average rotational speed of the two driving wheels which is equals the input rotational speed of the drive shaft. An increase in the speed of one wheel is balanced by a decrease in the speed of the other wheel.

Heavy vehicle transmission systems are subjected to noise and vibration under excitation condition. Internal excitation forces, meshing forces, load and speed variation and gear defects are one of the major sources of excitation. Automobile differential gearbox is an assembly of gears to meet the torque variation for dividing the speed of the wheel on turning conditions. The speed at the input shaft is maximum which is minimise at output shaft to increase torque value. High value of torque is transmitted to drive shaft. Noise and vibration reduction in heavy vehicle transmission system is a constant development, because noise and vibration are the two reasons for transmission failure. Mechanical properties of material influence the vibration signature pattern. The simulation results show that natural frequencies and mode shapes show different characteristics as we change the materials. Grey cast iron have damping property to reduce the vibration effect so it is used as automobile casing materials but structural steel have high density, it is used as casing material for heavy static machinery in industrial application.

Research Aim

- To design a gear box housing under the plateform of solodwork.
- To findout the natural frequencies of gearbox under different condition through ansys 14.0.
- To findout the stress and torque gererated in gearbox under different conditions.

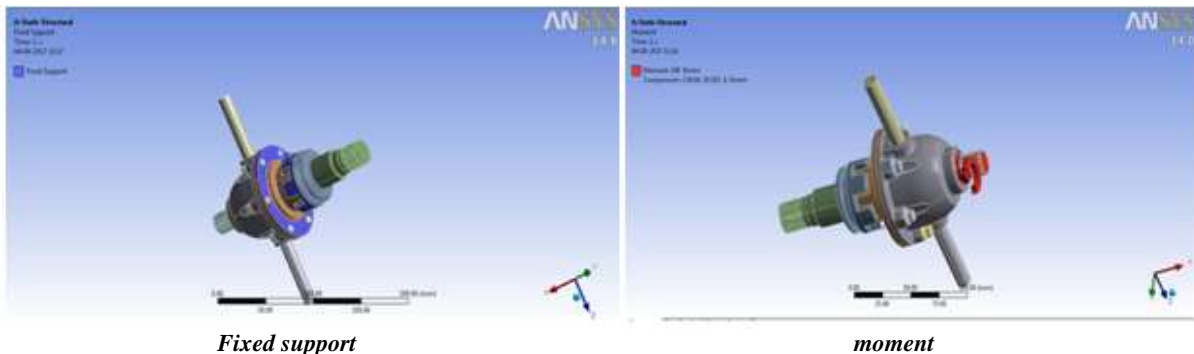
Analysis work

The project is divided into two domains:

1. Modal Analysis
2. Stress analysis

Modal Analysis: Natural frequencies of system are those frequencies at which the resonant response occurs under the right excitation conditions. Knowledge of these critical dynamic frequencies is an essential step in the design or evaluation of a system subjected to dynamic loading.

Stress Analysis: stress analysis is a part of static analysis of the model in ansys 14.0 and modeled in SOLIDWORKS by applying boundary conditions and forces which are calculated by the data provided by the instructor .



- 1.1 **Model analysis** it is a term used to describe the processes employed to extract a structure's modal properties (natural frequencies, modal damping factors, and mode shapes) from information about the structure that can be presented in a different form of formats. When these properties are extracted from a theoretical analysis of the dynamic behavior
- 1.2 **Gear mesh frequency** This type of frequency most commonly used with the gears & it is equal to the number of teeth on the gear multiple of the running speed of its shaft. A typical gearbox will have multiple gears and therefore multiple gear meshing frequencies. A normal gear mesh signature having low amplitude of gear mesh frequency with a series of symmetrical sidebands, spaced at the exact running speed of the shaft, on each side of the mesh components. The spacing and amplitude of these side bands is likely symmetrical if the operation of gearbox is normal. Any deviation in the symmetry of the gear mesh signature is an indication of incipient gear problems.

Modeling of gear

Modeling is a consistent set of principles for mathematical and computer modeling of three dimensional solids. Solid modeling is distinguished from related areas of geometric modeling and computer graphics by its emphasis on physical fidelity. Together, the principal of geometric and solid modeling form the foundation of computer aided design and in general support the creation, exchange, visualization, animation, interrogation, and annotation of digital models of physical objects.

II. CALCULATIONS OF A CROWN GEAR AND PINION

The main aim of the project is to verify the best material for the gears in the gear box at higher speeds by analyzing stress, displacement and also by considering weight reduction focus on the mechanical design and contact analysis on assembly of gears in gear box when they transmit power at different speeds at 2400 rpm, 5000 rpm and 6400 rpm. Analysis is also conducted by varying the frequencies. Differential gear is modeled in Solidwork . The ANSYS 14.0 fem software were used as the analysis tool for determining the structural behaviour of various composites under the given loading conditions.

Specifications Of Used Heavy Vehicle

ASSUMPTIONS:

- Gear profile: -20 degree full depth involute profile (standard)
- pressure angle (α): -20 degree

- bevel gear arrangement = 90 degree
- Pitch cone Angle (ϕ) = 45
- Back cone Angle (β) = 45
- Module (M) = 10
- Number of teeth on gear = $Z_g = 50$
- Number of teeth on pinion = $Z_p = 8$

Velocity Ratio (V.R)

$$V.R = TG/TP = DG/DP = NP/NG$$

$$V.R = TG/TP = 50/8 = 6.25$$

$$V.R = NP/NG$$

$$6.25 = 2400/NG$$

$$NG = 384 \text{ rpm}$$

Minimum no. of teeth on pinion (Z_p)

For satisfactory operation of bevel gears the number of teeth in the pinion must not be less than hence the assumed value of the pinion is in safe condition

Pitch circle diameter (D)

$$\text{Pitch circle diameter for the gear } (D_g) = M \cdot Z_g$$

$$\text{Pitch circle diameter for the pinion } (D_p) = M \cdot Z_p$$

Pitch angle (θ)

Since the shafts are at the right angles, the pitch angle were given as:

$$\text{For the pinion } = \theta_{p1} = \tan^{-1}(1/v.r)$$

$$\text{Pitch angle of gear } \theta_{p2} = 90^\circ - \theta_{p1} = 81^\circ$$

formative number of teeth (T_e)

$$\text{for the pinion } Z_{ep} = Z_p \sec \theta_{p1} = 8 \sec 9^\circ = 8$$

$$\text{for the gear } = Z_{eg} = Z_g \sec \theta_{p2} = 50 \sec 81^\circ = 319.622$$

1. Pitch Cone Distance (AO):

$$AO = ((d_1/2)^2 + (d_2/2)^2)^{1/2}$$

$$AO = 250 \text{ mm}$$

2. Face width (b)

$$b = AO/3$$

or } which is lesser

$$b = 10$$

III. CALCULATION OF GEAR AND PINION

1. Pitch circle diameter (D)

$$\text{Diameter of sungear } = D_g = 150 \text{ mm}$$

$$\text{Diameter of pinion } = D_p = 70 \text{ mm}$$

2. Number of tooth on gear

$$\text{Number of teeth on gear } = Z_g = 18$$

$$\text{Number of teeth on pinion } = Z_p = 15$$

$$D = D_g + D_p = 220$$

$$T = Z_g + Z_p = 33$$

3. Module = $M = D/T = 220/33 = 6.66 = 7$ (according to stds)

4. Velocity Ratio

$$V.R = Z_g/Z_p = DG/DP = NP/NG$$

$$V.R = D_g/D_p = 150/70 = 2.142$$

$$V.R = NP/NG$$

$$2.142 = 2400/NG$$

$$NG = 1120.448 \text{ rpm}$$

[Pandey * *et al.*, 6(9): September, 2017]
 ICTM Value: 3.00

5. Pitch angle

Since the shafts are at right angles therefore pitch angle

for the pinion = $\theta_{p1} = \tan^{-1}(1/v.r)$

= $\tan^{-1}(1/2.142) = 25.025$

Pitch angle of gear $\theta_{p2} = 90^\circ - 25.025 = 64.974$

6. Formative Number Of Teeeth

For the pinion = $Z_{ep} = Z_p \sec\theta_{p1} = 15 \sec 25.025 = 16.554$

For the gear = $Z_{eg} = Z_g \sec\theta_{p2} = 8 \sec 64.974 = 42.55$

7. Pitch Cone Distance (AO):

$AO = ((D_1/2)^2 + (D_2/2)^2)^{1/2}$

AO = 82.7mm

8.Face Width (b): $82.7/3 = 27.5$ mm

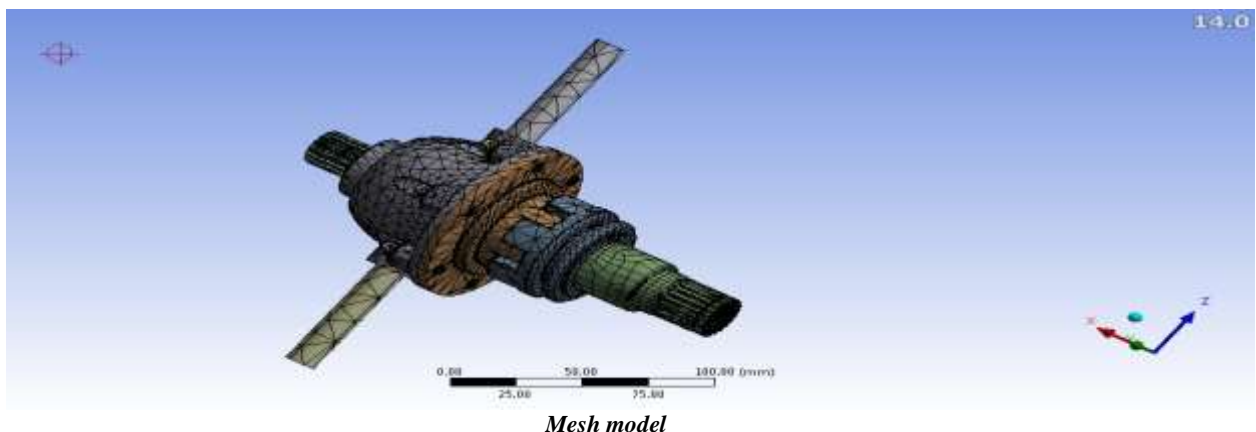
IV. FEM ANALYSIS OF THE GEAR

The finite element method (FEM) is a numerical method by which we can solve problems of engineering and mathematical physics. FEM is also known as finite element analysis (FEA). Complex problem areas of interest that contain structural analysis, heat transfer, fluid flow, mass transport, and electromagnetic potential. The analytical method of solution generally requires solution to boundary problems for partial differential equations. This method is formulation of the problem results in a system of algebraic equations. The yields approximate values of the unknowns at discrete number of points over the domain.¹ To solve these problem, it is subdivides large problem into smaller and simpler parts that are called finite elements. The simple equations that model these finite elements are then assembled into a larger system of equations that models the entire problem. FEM then uses variational methods from the calculus of variations to approximate a solution by minimizing an associated error function.

V. MESHING OF GEAR ASSEMBLY

A mesh is the Discretization of a component into a number of small elements of defined size. Finite element analysis is dividing the geometry into various small number of elements. These elements are connected to each other at a point called nodes. Each node may have two or more than two elements connected to it. A collection of these elements is called mesh.

Meshing is very important part of pre-processing in any FEA software. In ANSYS workbench there are many tools and option available to help for create an mesh.



[Pandey * *et al.*, 6(9): September, 2017]
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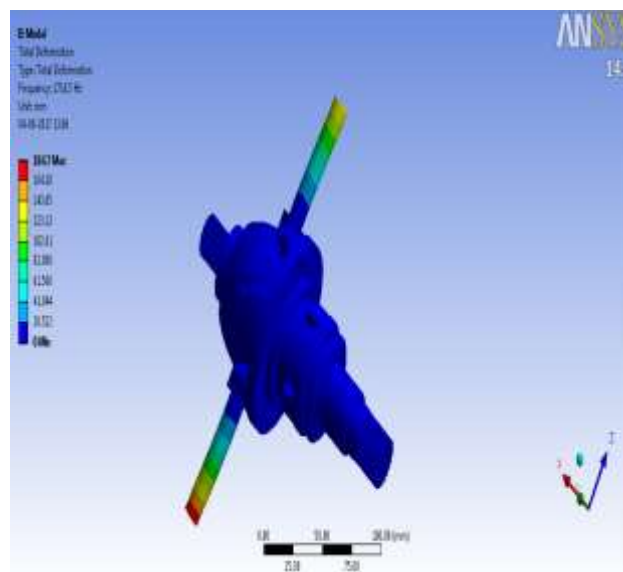
Problem formulation

A natural frequency, epitomized by resonance, is the characteristic of the part or subassemblies of a required product. This becomes noticeable while assessing performances of applications where human comfort of the component life has a prominence on the function. Automobiles for example, are subjected to vibrations in terms of road caused by the engine. The components making up the subassemblies need to be evaluated for this phenomenon. The design of the component should incorporate a mode for dealing with factors causing undesirable levels of vibration or to support any scientific means of problem solving that would decrease the harmful effects of resonance.

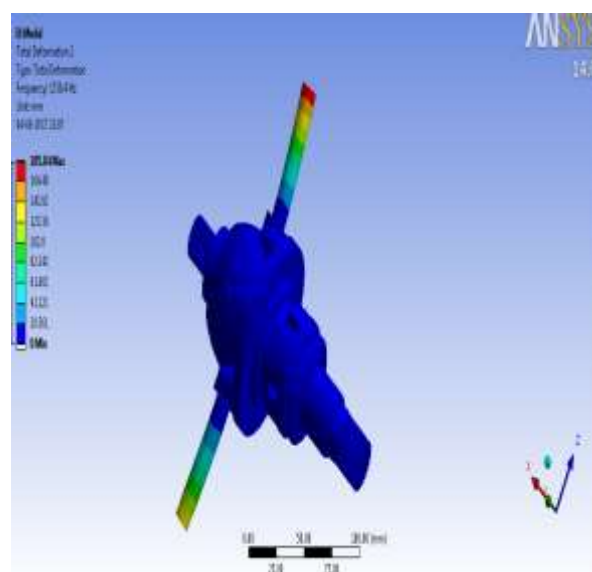
VI. RESULT

Modal analysis

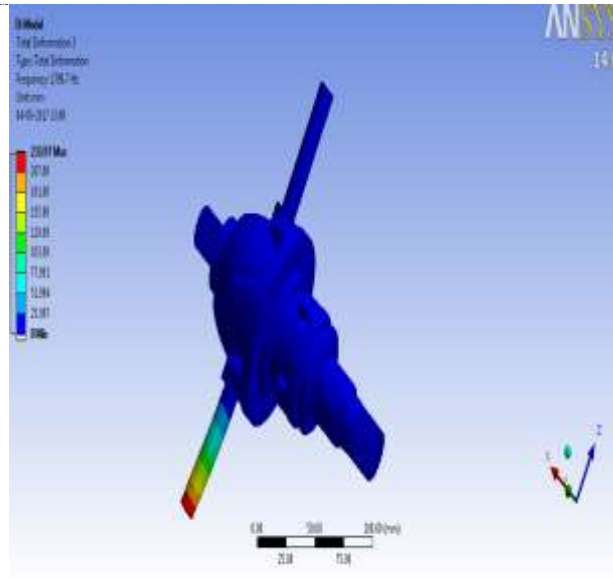
After analysis of all the stresses and formulation the following natural frequencies are obtained



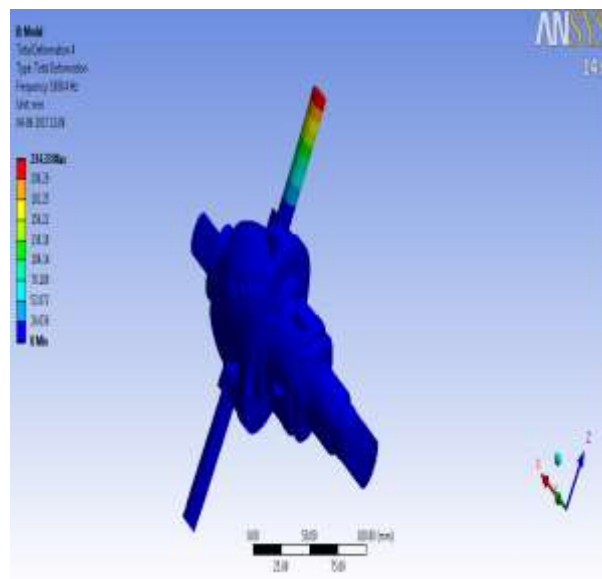
Total deformation 1



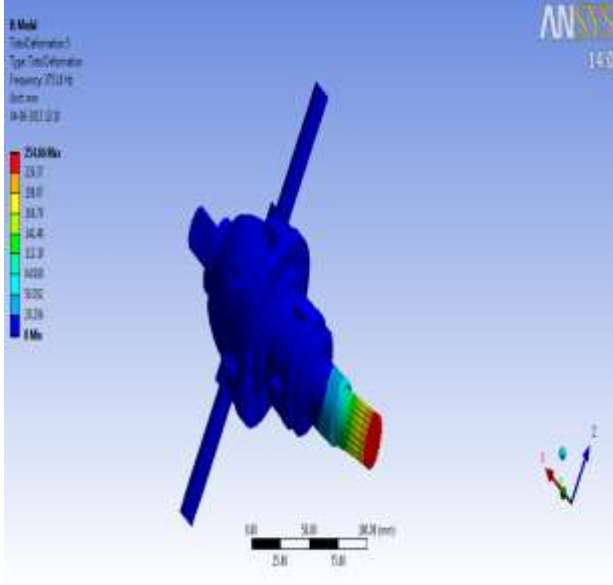
Total deformation 2



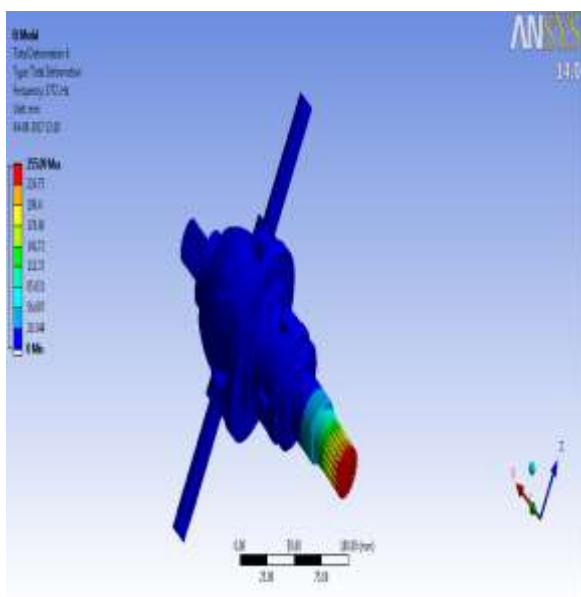
Total deformation 3



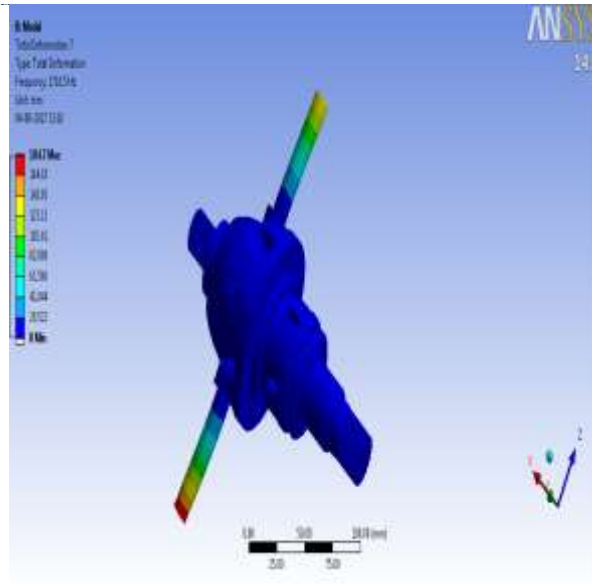
Total deformation 4



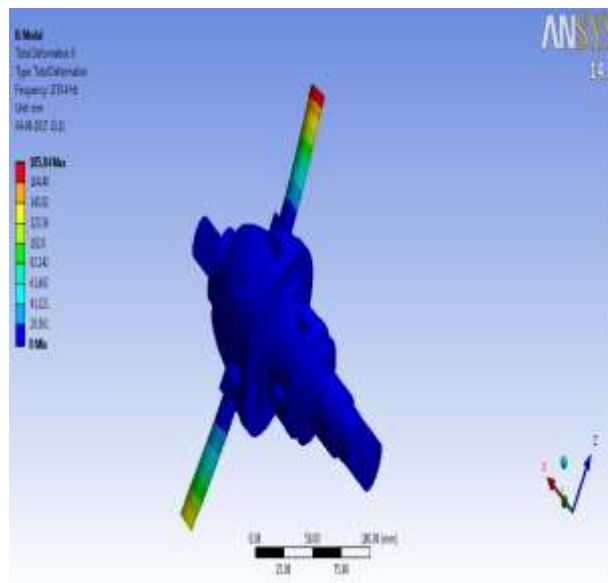
Total deformation 5



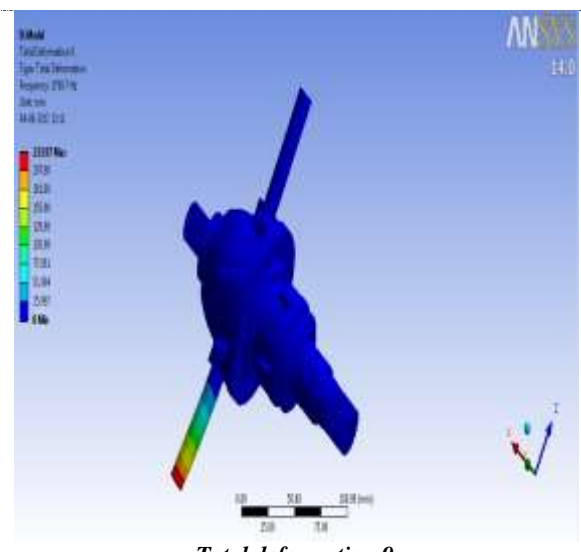
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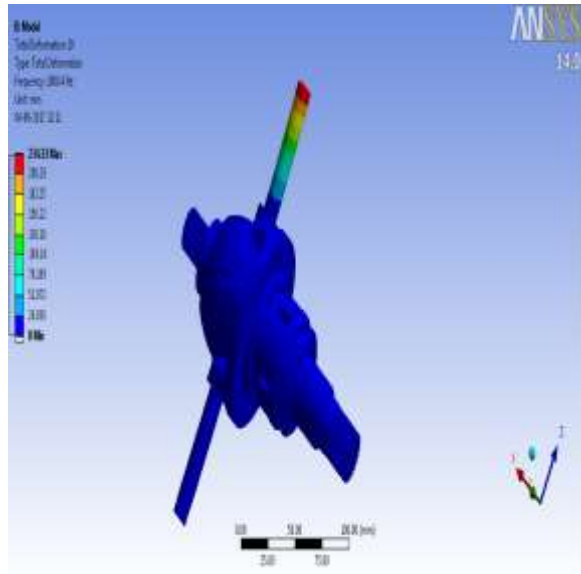
Total deformation 7



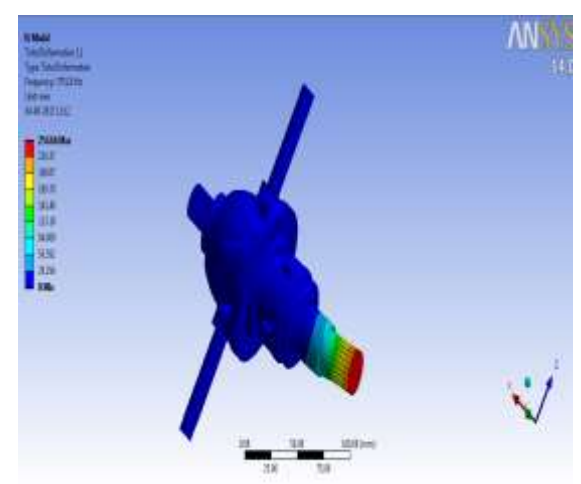
Total deformation8



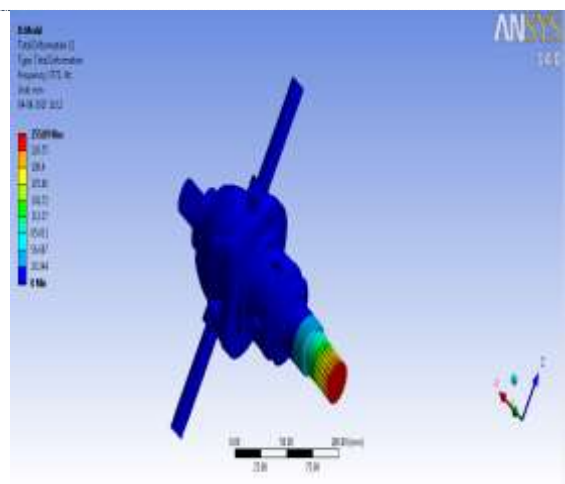
Total deformation 9



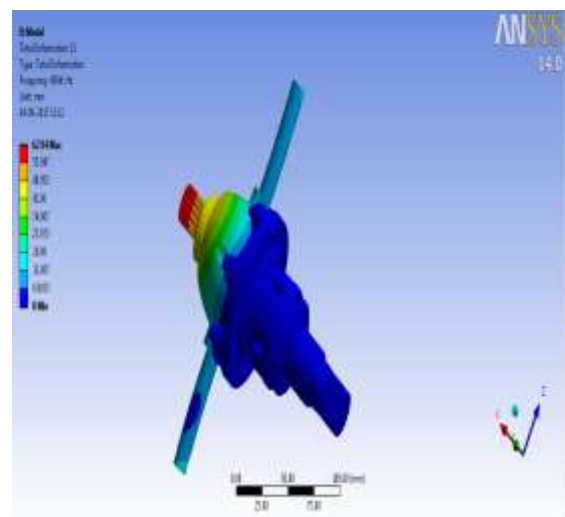
Total deformation 10



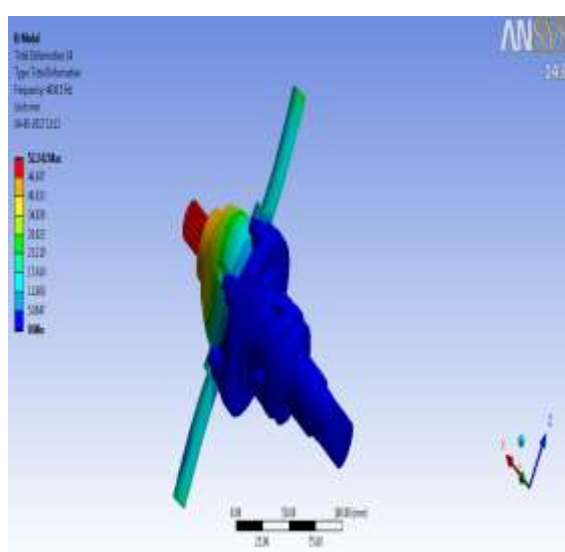
Total deformation 11



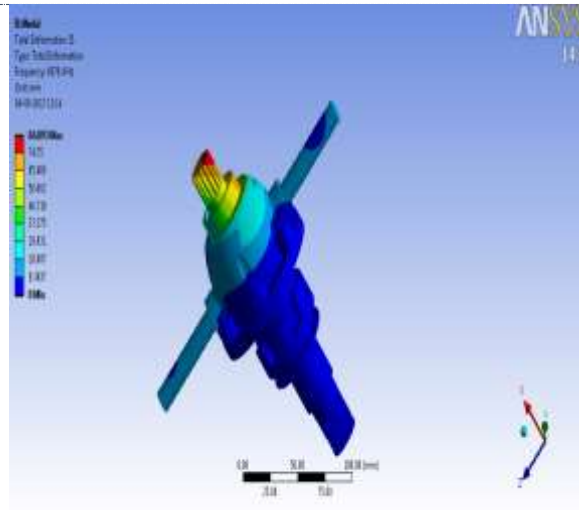
Total deformation 12



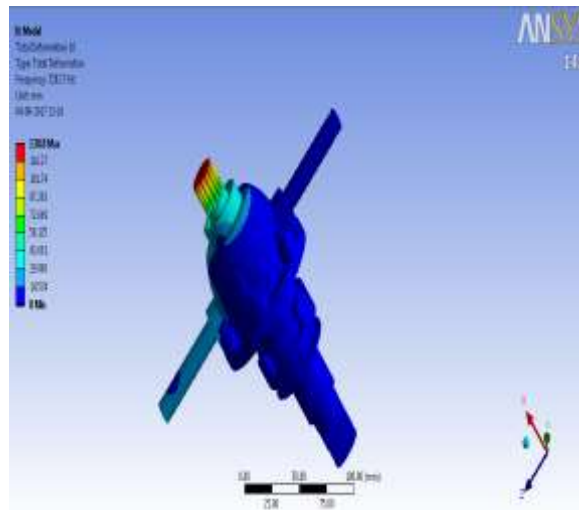
Total deformation 13



Total deformation 14



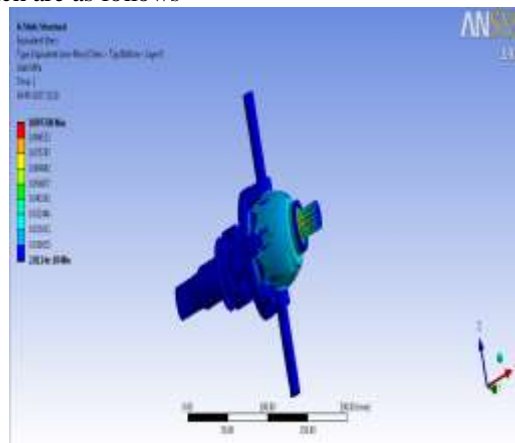
Total deformation 15



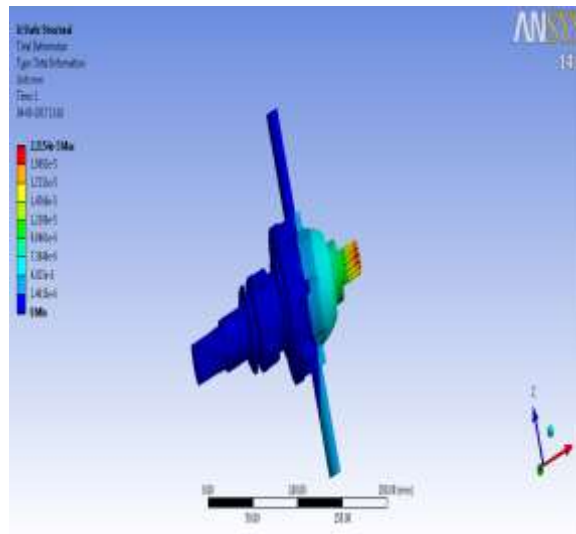
Total deformation 16

VII. STRESS ANALYSIS

As we know high contact stresses are results in pitting failure of the gear tooth, it is compulsory to keep contact stresses within the limit. After analysis of the differential gear assembly the stress and moment on different modes it has been obtained which are as follows



Deformation due to stress



deformation due to torque

VIII. CONCLUSION

In this research 3-D deformable-body model of differential gearbox and its housing was developed through SOLIDWORKS. The results obtained were then compared with the AGMA theoretical stress values. The results are in good congruence with the theoretical values, which suggest that the model designed is correct. after the analysis the following frequencies are obtained:-

Mode	Frequency [Hz]
1.	1716.5
2.	1730.4
3.	1790.7
4.	1800.4
5.	3751.8
6.	3772.
7.	4594.
8.	4630.5
9.	6979.4
10.	7282.7

IX. REFERENCES

- [1] AnoopLega, PuneetKatyal, Vishal Gulati, 'Computed Aided Design and Analysis of Composite Gearbox Material', International Journal of Mechanical Science and Civil Engineering (IJMSCE), Volume-1, Issue- 1, December 2012, page.
- [2] Bracci, M. Gabiccini, A. Artoni, M. Guiggian, 2009, 'Geometric contact pattern estimation for gear drives', Computer Methods in Applied Mechanics and Engineering, Volume 198, Issues 17–20, 15 April 2009, Pages 1563-1571.
- [3] B.Venkatesh, V.Kamala, A.M.K.Prasad, 2010, 'Modelling and Analysis of Aluminium A360 Alloy Helical Gear for Marine Applications', International Journal Of Applied Engineering Research, Dindigul Volume 1, No 2, 2010, page. 124-134.
- [4] C. Fetvaci, 2010, 'Definition of Involutes Spur Gear Profiles Generated by Gear-Type Shaper Cutters', Mechanics Based Design of Structures and Machines: An International Journal, Vol. 38, No. 4, page. 481- 492.
- [5] C.Veeranjaneyulu, U. HariBabu , 2012, 'Design And Structural Analysis of Differential Gear Box at Different Loads' , International Journal of Advanced Engineering Research and Studies, Vol. 1, Issue II, January-March, 2012, page. 65-69.

- [6] CuneytFetvaci&ErdemImrak, 2008, 'Mathematical Model of a Spur Gear with Asymmetric Involute Teeth and Its Cutting Simulation', Mechanics Based Design of Structures and Machines: An International Journal, Vol. 36, No. 1, page. 34-46.
- [7] Chabra Pankaj , Bhatia Amit , "Design and Analysis of Composite Material Gear Box", International Journal of Mechanical and Civil Engineering, Vol.1(2012), Issue1,pp 15-25.
- [8] Dong Yang, Huanyong Cui, XijieTian, Qingping Zhang and PengfeiXu, 2011, 'Research on Tooth Modification of Spur Bevel Gear', the Open Mechanical Engineering Journal, 2011, 5, page. 68-77.
- [9] Devi Neelima, Mahesh.V, Selvaraj. N., "Mechanical characterization of Aluminium silicon carbide composite", International Journal Of Applied Engineering Research, Volume 1(2011), Issue No 4,pp126- 131.
- [10]Erwin V. Zaretsky, David G. Lewicki, Michael Savage & Brian L. Vlcek 25, 2008, 'Determination of Turboprop Reduction Gearbox System Fatigue Life and Reliability', ISSN Taylor & Francis, Tribology Transactions, 50:4, page. 507-516.
- [11]F. K. Choy, H. Chen & J. Zhou, 2006, 'Identification of Single and Multiple Teeth Damage in a Gear Transmission System', Tribology Transactions, Vol. 49, No. 3, page. 297-304.
- [12]Gulaxea Pratik , Awate N.P.,"Design, Modelling & Analysis of Gear Box for Material Handling Trolley: A Review", Mechanica Confab, Vol 2, Issue1,(2013),pp63-70.
- [13]Gintin mitra , " the hand book of gear design "SECOND EDITION Tata McGraw-Hill Publishing Company Limited NEW DELHI.
- [14]Hashim J.,Looney L Hashmi M.S.J., Metal Matrix Composites: Production by the Stir Casting Method, Journal of Material Processing and Technology,(1999),pp. 17.
- [15]IsadŠarić; AdilMuminović, 2010, 'Parameter Modelling of Gear', International Research/Expert Conference, "Trends in the Development of Machinery and Associated Technology", TMT 2010, Mediterranean Cruise, 11-18 September 2010, page. 557-560.
- [16]Lei Wang, Jiancheng Yang &Xiaoqin Han, 2009, 'The Performance Study of Hybrid-driving Differential Gear Trains', Modern Applied Science, vol. 3, No. 9, page. 95-102.
- [17]R. Yakut, H. Duzcukoglu, M. T. Demirci, " The load capacity of PC/ABS spur gears and investigation of gear damage", Archives of Materials science and Engineering, November 2009, 40/1, page 41-46.
- [18]Riccardo Morselli a , Roberto Zanasi a &GermanoSandoni, 2006, 'Detailed and reduced dynamic models of passive & active limited-slip car differentials' ISSN Taylor & Francis, Vol. 12, No. 4, Aug 2006, page. 347 – 362.
- [19]V. Siva Prasad, Syed Altaf Hussain, V. Pandurangadu, K. PalaniKumar, " Modeling and Analysis of spur gear for Sugarcane Juice Machine under Static Load Condition by Using FEA",July-Aug 2012,International Journal of Modern Engineering Research,Vol- 2/4, pp-2862-2866.
- [20]Vivek Karaveer*, Ashish Mogrekar and T. Preman Reynold Joseph, " Modelling and Finite Element Analysis of Spur Gear", Dec 2013, International Journal of Current.

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