A Novel High-Gain DC-DC Converter Applied in Fuel Cell Vehicles

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Abstract—The DC-DC converter for fuel cell vehicles should be characterized by high-gain, low voltage stress, small size and high-efficiency. However, conventional two-level, three-level and cascaded boost converters cannot meet the requirements. A new non-isolated DC-DC converter with switched-capacitor and switched-inductor is proposed in this paper, which can obtain high-gain, wide input voltage range, low voltage stresses across components and common ground structure. In this paper, the operating principle, component parameters design, and comparisons with other high-gain converters are analyzed. Moreover, the state-space averaging method and small-signal modeling method are adopted to obtain the dynamic model of converter. Finally, simulation and experimental results verify the effectiveness of the proposed topology. The input voltage of the experimental prototype ranges from 25V to 80V. The rated output voltage is 200V and rated power is 100W. The maximum efficiency is 93.1% under rated state. The proposed converter is suitable for fuel cell vehicles.

Index Terms—Fuel cell vehicles, DC-DC converter, switched-capacitor and switched-inductor, high-gain, low voltage stress.

I. INTRODUCTION

The development of the transportation industry plays a vital role in the national economy. However, an increase in the number of fuel vehicles not only consumes a large amount of oil resources, but also causes serious environmental pollution problems. Therefore, all countries turn their attentions to the clean energy [1], [2]. The development of new energy vehicle industry provides new ideas to solve these problems. Fuel cell vehicle has become a very promising development direction in the new energy vehicle industry due to its advantages of zero emissions, no pollution and high efficiency [3], [4].

The typical system structure of fuel cell vehicle is shown in Fig. 1. The low output voltage of fuel cell makes it difficult to meet the demand of DC bus voltage in front of inverter. Moreover, the fuel cell has a "soft" output voltage characteristic, i.e., the output voltage drops too fast with the increase of the output current [5], [6]. Therefore, the DC-DC converter with high-gain, wide input voltage range and small size should be applied to fuel cell vehicles to raise the fuel cell voltage to a higher voltage level and ensure the stability of the DC bus voltage.

Isolated DC-DC converter can easily achieve high-gain by changing the transformer turns ratio. However, due to the leakage inductance of the transformer, the circuit will produce a peak voltage, which is easy to breakdown the devices in the circuit. The leakage inductance can also reduce the efficiency of the converter and cause electromagnetic interference problems. In addition, transformer in the isolated converter also increases the size of the converter [7], [8]. Considering the size, cost and efficiency, the non-isolated DC-DC converter is more suitable for fuel cell vehicles.

The traditional boost DC-DC converter is still used in many applications because of the small number of components and simple structure. The theoretical voltage gain of the boost converter is \(1/d\), where \(d\) is the duty cycle of the drive voltage for power switch. However, the voltage gain is limited due to the parasitic parameters of the actual circuit and components. The voltage stresses across components in the circuit are also high, which needs more expensive high-voltage components, resulting in increased size and cost [9]. In addition, there is an extreme duty cycle in traditional boost converter when achieving high-gain, which causes serious diode reverse recovery problems, resulting in increased losses [10], [11]. In terms of these disadvantages, conventional boost converter is not suitable for fuel cell vehicles. The cascaded boost converter can achieve high-gain and wide input voltage range by sacrificing the overall power density and efficiency of converter, but the voltage stresses across components are high and the circuit structures are complex [12], [13]. The boost three-level DC-DC converter can reduce the voltage stresses across components, but the voltage gain is still as low as the conventional boost converter [14].

In [15], the voltage stresses across components are significantly reduced and the theoretical voltage gain can reach \((1+d)/(1-d)\), which is slightly larger than the conventional boost converter. However, the voltage gain in [15] is still not
enough for fuel cell vehicles. Z-source and quasi-Z-source networks are applied to the DC-DC converter to obtain the high-gain, but the voltage stresses of components in the converter are still high [16], [17]. In [18], a converter based on a series structure of three Z-source networks is proposed, which can obtain high-gain, wide input voltage range and low stress. However, there are too many inductors and power semiconductors in the circuit, which increases the cost and size of the converter. The converters proposed in [19]–[21] can achieve high-gain and low voltage stress, but there is a non-common ground structure between the input and output ports of each converter. When the converter is working, there is a high frequency pulsed voltage between the input and output ports, which can cause serious EMI problems. In addition, the main problem is about the voltage feedback for the non-common ground structure. An isolated voltage feedback should be adopted, such as: linear optocoupler, which can increase the complexity of the sampling circuit [22]. The multi-level converters proposed in [23], [24] can achieve high-gain and low voltage stresses across components. However, there are too many power semiconductors in the the circuit, resulting in increased cost and size. Multiple power switches also increase complexity to the drive circuit and control strategy. The non-isolated converters with coupled-inductor proposed in [25]–[27] can easily achieve high-gain, reduce the size of inductor and increase the power density of the converter. However, due to the existence of leakage inductance, additional clamp circuit or absorption circuit should be adopted to absorb the leakage inductance energy, which increases the complexity of the converter.

In this paper, a DC-DC converter based on switched-capacitor and switched-inductor is proposed. The converter can obtain high-gain, wide input voltage range, low voltage stress and common ground structure between input and output ports. In addition, there is no extreme duty cycle and the power switches need only one PWM drive signal in circuit topology. This paper is organized as follows: In Section II, the operating principle, voltage gain and voltage stresses across components are analyzed. And the converter is also compared with other high-gain DC-DC converters. In section III, the component parameters are designed. The dynamic model of the converter is presented by using state-space averaging method and small-signal modeling method. In Section IV and Section V, the simulation and experimental results are presented respectively to verify the effectiveness of proposed converter. Finally, the conclusion is given in Section VI.

II. PRINCIPLE OF THE PROPOSED CONVERTER

A. Configuration of the Proposed Converter

The circuit topology of the proposed converter is shown in Fig. 2. $U_{in}$ and $U_0$ are the input voltage and output voltage respectively. $R_L$ is the load resistance. The converter consists of two power switches ($Q_1, Q_2$), five diodes ($D_1, D_3, D_6$), four capacitors ($C_1-C_4$) and an inductor $L$. $Q_1$ and $Q_2$ are turned on and off simultaneously by using the same gate drive signal $S$.

When power switches $Q_1$ and $Q_2$ are turned on, $S=1$, and vice versa, calling $S=0$.

![Fig. 2. The circuit topology of the proposed converter.](image)

B. Operating Principle of the Proposed Converter

In order to analyze the proposed converter topology, some assumptions are made as follow:

a) The forward voltage drop of diode and the on-state resistance of power switch are ignored. The equivalent series resistances of inductor and capacitors are equal to 0.

b) The inductor is large enough in order to ensure that the circuit works normally. The capacitors are large enough in order to ensure that the voltage ripple of capacitors meets the requirements in this paper.

In this paper, the operating principle in Continuous Conduction Mode (CCM) is analyzed. The key operating waveforms of the proposed converter in CCM are shown in Fig. 3. According to the switching states of power switches, there are two operating states for the proposed converter, as shown in Fig. 4.

![Fig. 3. The key operating waveforms of proposed converter in CCM.](image)
When power switches \( Q_1 \) and \( Q_2 \) are turned off (\( S=0 \)), the equivalent circuit is shown in Fig. 4(b), defined as OFF state. The diode \( D_1 \) is reverse biased and four current loops appear in the circuit. Inductor \( L \) charges capacitor \( C_1 \) through \( D_1 \) and \( D_2 \). \( U_{in} \) and \( L \) charge capacitor \( C_4 \) through \( D_1 \) and \( D_2 \). \( U_{in}, L \) and \( C_2 \) charge the series part of \( C_3 \) and \( C_4 \) through the diodes \( D_1 \) and \( D_2 \). The series part of the capacitors \( C_1 \) and \( C_4 \) still transfers energy to the load \( R_L \).

![Diagram](image)

**Fig. 4.** Two operating states of the proposed converter. (a) ON state. (b) OFF state.

### C. Analysis of Voltage Gain and Voltage Stress

Equations (1) and (2) can be obtained by applying Kirchhoff’s Voltage Law (KVL) and Kirchhoff’s Current Law (KCL) to the circuit topology in Fig. 4(a).

\[
\begin{align*}
U_{L(ON)} &= U_{in} + U_{C1} \\
U_{C2} &= U_C \\
U_0 &= U_{C3} + U_{C4}
\end{align*}
\]

where \( U_{C1}, U_{C2}, U_{C3} \) and \( U_{C4} \) are the capacitor voltages across \( C_1, C_2, C_3 \) and \( C_4 \) respectively. \( U_{L(ON)} \) is the inductor voltage across \( L \) when the converter operates in ON state. \( U_0 \) is the output voltage of the converter.

\[
\begin{align*}
I_{C1(ON)} &= -I_L \\
I_{C2(ON)} &= I_{C3(ON)} - I_{C4(ON)} \\
I_{C3(ON)} &= -I_0
\end{align*}
\]

where \( I_L \) is the average current of inductor \( L, I_{C1(ON)}, I_{C2(ON)}, I_{C3(ON)}, \) and \( I_{C4(ON)} \) are the average currents of the capacitors \( C_1, C_2, C_3 \) and \( C_4 \) respectively, when the converter operates in ON state. \( I_0 \) is the load current.

Equations (3) and (4) can be obtained by applying KVL and KCL to the circuit topology in Fig. 4(b).

\[
\begin{align*}
U_{L(OFF)} &= -U_{C1} \\
U_{C4} &= U_{in} - U_{L(OFF)} \\
U_0 &= U_{in} - U_{L(OFF)} + U_C \\
U_0 &= U_{C3} + U_{C4}
\end{align*}
\]

where \( U_{L(OFF)} \) is the inductor voltage across \( L \) when the converter operates in OFF state.

\[
\begin{align*}
\{I_{C1(OFF)} &= I_L + I_{C2(OFF)} + I_{C3(OFF)} - I_{C4(OFF)} \\
I_{C2(OFF)} &= -I_0 - I_{C3(OFF)} \}
\]

where \( I_{C1(OFF)}, I_{C2(OFF)}, I_{C3(OFF)}, \) and \( I_{C4(OFF)} \) are the average currents of the capacitors \( C_1, C_2, C_3 \) and \( C_4 \) respectively, when the converter operates in OFF state.

Equation (5) can be obtained by applying the voltage-second balance principle to inductor \( L \), and equation (6) can be obtained by applying the amper-second balance principle to capacitors \( C_1, C_2, C_3 \) and \( C_4 \).

\[
\begin{align*}
U_{L(ON)} \times dT + U_{L(OFF)} \times (1-d)T &= 0 \quad (5) \\
I_{C1(ON)} \times dT + I_{C1(OFF)} \times (1-d)T &= 0 \\
I_{C2(ON)} \times dT + I_{C2(OFF)} \times (1-d)T &= 0 \\
I_{C3(ON)} \times dT + I_{C3(OFF)} \times (1-d)T &= 0 \\
I_{C4(ON)} \times dT + I_{C4(OFF)} \times (1-d)T &= 0
\end{align*}
\]

where \( d \) is duty cycle of power switches \( Q_1 \) and \( Q_2 \). \( T \) is the switching period.

In terms of (1), (3) and (5), the theoretical voltage gain \( M \) of the converter can be obtained as shown in (7).

\[
M = \frac{U_0}{U_{in}} = \frac{2(1-d)}{1-2d} \quad (7)
\]

where \( 0<d<0.5 \). The proposed converter cannot work normally if \( d>0.5 \).

In terms of (1), (3), (5) and Fig. 4, the voltage stresses across all capacitors and power semiconductors in the circuit topology are obtained as shown in (8).

\[
\begin{align*}
U_{C1} &= U_{in} = U_{Q1} = U_0/2 - U_{in} \\
U_{C2} &= U_{C3} = U_{C4} = U_{in}/2 \\
U_{Q2} &= U_{in}/2
\end{align*}
\]

From (7), the converter can obtain a high-gain and the duty cycle \( d \) is always less than 0.5 without extreme duty cycles. From (8), the voltage stresses of all capacitors and power semiconductors in the circuit topology are no more than \( U_0/2 \), which is beneficial to reducing size, cost and improving efficiency of the converter.

Assuming that the input power of the converter is equal to the output power in the ideal state, equation (9) can be obtained.

\[
U_{in} \times I_{in} = U_0 \times I_0 \quad (9)
\]

where \( I_{in} \) is the average input current of the converter.

In terms of (2), (4), (6), (9) and Fig. 4, the inductor current \( I_L \) is obtained as shown in (10) and the current stresses of all capacitors in the circuit topology are obtained as shown in (11).

\[
I_L = \frac{2}{1-2d} I_0 \quad (10)
\]
Two converters for fuel cell vehicles are proposed in [28] and [29] with low voltage stress and wide input voltage range. The voltage stresses across all components are reduced to $U_{O/2}$ and the voltage gain ($M=2/(1-d)$) is twice better than the conventional boost converter. But the voltage gain is lower than that of the proposed converter in this paper, and these two converters may suffer from extreme duty cycles when high-gain is achieved. Furthermore, the circuit topologies are non-common ground structure and there is a potential difference equal to $U_{O/2}$ between the input and output ports in each converter, which can cause safety problems. Although this potential difference is not a high frequency pulsated voltage, the non-common ground structure also bring difficulty to the sampling of the output voltage. The converter in [30] can obtain low voltage stresses across components and the operating range of $d$ is from 0.5 to 0.75. However, the voltage gain is still low and there is an extra inductor in circuit topology compared with the proposed converter in this paper.

In terms of (10), (11) and Fig. 4, the current stresses of all power semiconductors are obtained as shown in (12).

$$
\begin{align*}
I_{Q1} = I_{D1} &= -I_{C1(ON)} = \frac{2}{1-2d} I_o \\
I_{Q2} = I_l + I_{C2(ON)} &= \frac{1}{d(1-2d)} I_o \\
I_{D2} &= -I_{C1(OFF)} = \frac{-2d}{(1-d)(1-2d)} I_o \\
I_{D3} &= I_{C4(OFF)} - I_{C3(OFF)} = \frac{1}{1-d} I_o \\
I_{D4} &= I_{C2(ON)} = -I_o \\
I_{D5} &= I_o + I_{C3(OFF)} = \frac{1}{1-d} I_o
\end{align*}
$$

The MOSFET is adopted as power switch in experimental prototype of the proposed converter. Because the MOSFET and Schottky diode are suitable for low voltage and large current applications, this paper is only concerned with the voltage stresses of the components. The current stresses of the components are only used as an auxiliary reference for later component selection.

D. Comparisons With Other Converters

The proposed converter is compared with other converters in terms of voltage gain, voltage stress, the number of components, and common ground structure, as shown in Table I. The relationships between voltage gain $M$ and duty cycle $d$ among different converters are shown in Fig. 5.

Compared with conventional boost converter, the proposed converter can obtain a higher gain. When the proposed converter achieves high-gain, the duty cycle is always less than 0.5 without extreme duty cycle. Furthermore, the voltage stresses across components of the proposed converter are no more than $U_{O/2}$, rather than the $U_O$ of conventional boost converter. The low voltage-stress can reduce the volume and cost of the capacitors, which occupy large volume of converter. The low voltage-stress can also reduce the voltage breakdown risk of the device and improve the reliability of the converter.

Compared with the traditional quasi-Z-source converter ($M=1/(1-2d)$), the voltage gain of the proposed converter ($M=2(1-d)/(1-2d)$) is always larger than that of the traditional quasi-Z-source converter within $0<d<0.5$ and the smaller $d$ is, the greater voltage gain difference is. The voltage stresses across components of the proposed converter are no more than $U_{O/2}$, rather than the $U_O$ of quasi-Z-source converter. The voltage gain of the converter in [31] is slightly greater than that of the proposed converter within $0.33<d<0.5$ and is smaller than that of the proposed converter within $0<d<0.33$. But the voltage gain of the proposed converter in this paper can meet the requirements of high-gain for fuel cell vehicles. In addition, the converter in [31] adopts a large number of inductors, which increase the size of the converter. The circuit topology is a non-common ground structure in [31] and there is a high frequency pulsed voltage between the input and output ports, which results in EMI problem.

The proposed converter can obtain high-gain, low voltage stresses across components. The common ground structure of proposed converter can also avoid EMI problem. In addition, the power switches can be driven by only one PWM driving signal, which is beneficial to reducing the complexity of driving

References


circuits. By using switched capacitor technique, there should be inrush current when the converter works at hard switching conditions. This problem can be suppressed by reducing the voltage differential between two capacitors, which can be achieved by increasing the switching frequency. Besides, soft-switching technique can also effectively suppress the EMI and inrush current caused by switched capacitor technique. Based on the comparison results among different converters, the proposed converter in this paper is more advantageous in terms of high-gain, wide input voltage range, low voltage stress and common ground structure.

III. PARAMETERS DESIGN AND DYNAMIC MODELING

A. Design of Inductor and Capacitors

In terms of the converter topology in Fig. 2, the inductor \( L \) can be calculated by (13).

\[
L = \frac{u_o}{\frac{dt}{dn}}. \tag{13}
\]

The maximum inductor current and the maximum duty ratio can be obtained when the input voltage is the lowest, that is \( U_{in}=25V \) in proposed converter. Therefore, the inductor is designed when \( U_{in}=25V \), \( U_o=200V \), \( f=20kHz \) and \( R_s=400\Omega \) in this paper. Assuming the current ripple of inductor \( L \) is \( \Delta I_L \), hence, the current ripple coefficient of inductor \( L \) is \( \gamma = \Delta I_L / I_L \).

In order to avoid excessive inductor current ripple, the ripple rate of inductor current is set as \( \gamma \leq 0.4 \). When the converter operates in the ON state as shown in Fig. 4(a), \( u_t=u_{in}+u_{c1} \), \( dt=dxT=dlf \). In terms of (7), (10) and (13), the calculation equation of inductance can be obtained as (14).

\[
L \geq f(1-2d)R_i \frac{4\gamma f}{1} = 750\mu H \tag{14}
\]

where \( f \) is the switching frequency of the converter and \( d \) is the duty cycle of the drive signal for power switches \( Q_1 \) and \( Q_2 \).

When \( R_i=400\Omega \) and \( U_{in}=200V \), the output current \( I_o=U_o / R_i=0.5A \). According to (10), \( I_o=7.14A \) can be obtained. When \( U_{in}=25V \) and \( U_o=200V \), the peak value of inductor current \( I_{L, peak} \) is obtained as shown in (15).

\[
I_{L, peak} = I_o + \frac{d}{2} = I_o + \frac{I_o \gamma}{2} = 8.6A \tag{15}
\]

The energy storage of the magnetic core is calculated as shown in (16).

\[ L \cdot I_{L, peak}^2 = 0.8mH \times (8.6A)^2 = 59.2mH \cdot A^2 \tag{16} \]

Considering the flux density and price, the ferro-silicon aluminum magnetic core is adopted in this paper. By referring to magnetic core selection curves of Magnetics company for the iron-silica-aluminum, the 77438 magnetic core is selected for inductor design in this paper.

The capacitor \( C \) can be calculated by (17). Assuming the voltage ripples of capacitors \( C_1, C_2, C_3, C_4 \) are \( \Delta U_{C1}, \Delta U_{C2}, \Delta U_{C3}, \Delta U_{C4} \), respectively. In terms of (11) and (17), the calculation equation of capacitance can be obtained as (18).

\[
C = \frac{d}{\frac{dt}{dC}} \tag{17}
\]

\[
C_1 = \frac{2dI_o}{(1-2d)\Delta U_{C1}f} \tag{18}
\]

\[
C_2 = \frac{I_o}{\Delta U_{C2}f} \tag{18}
\]

\[
C_3 = \frac{dI_o}{\Delta U_{C3}f} \tag{18}
\]

\[
C_4 = \frac{(1+d)I_o}{\Delta U_{C4}f} \tag{18}
\]

B. Dynamic Modeling Analysis

When the converter operates in the ON state, capacitors \( C_2 \) and \( C_4 \) are in parallel as shown in Fig. 4(a). The relationship between \( C_2 \) and \( C_4 \) is shown in (19), indicating that there is an invalid variable between \( C_2 \) and \( C_4 \).

\[
C_2 \frac{dU_{c2}}{dt} = -C_4 \frac{dU_{c4}}{dt} \tag{19}
\]

In order to eliminate the invalid variable between \( C_2 \) and \( C_4 \), the series equivalent resistance \( r_1 \) is introduced into \( C_2 \) and \( C_4 \) loop and equation (19) can be written as (20).

\[
C_2 \frac{du_{c2}}{dt} = -\frac{u_{c4}-u_{c2}}{r_1} \tag{20}
\]

where the \( r_1 \) is the equivalent series resistance in \( C_2 \) and \( C_4 \) loop, defined as \( r_1 = 0.01\Omega \).

When the converter operates in the OFF state, the series equivalent resistance \( r_2 = 0.01\Omega \) is adopted to eliminate the invalid variable of \( C_1, C_3, C_1 \) and \( C_4 \) loops as shown in Fig. 4(b). After adopting equivalent resistances \( r_1 \) and \( r_1 \), the equivalent circuit topology is as shown in Fig. 6.
\[
\frac{\text{d}u(t)}{\text{d}t} = \begin{bmatrix}
0 & 1/L & 0 & 0 & 0 \\
-1/C & 0 & 0 & 0 & 0 \\
0 & 0 & -1/rC & 0 & 0 \\
0 & 0 & 0 & -1/C_r & 0 \\
0 & 0 & 1/C_r & 0 & 0
\end{bmatrix}
\begin{bmatrix}
u_i(t) \\
u_c(t) \\
u_c(t) \\
u_c(t) \\
u_c(t)
\end{bmatrix}
+ \begin{bmatrix}
1 \\
0 \\
0 \\
0 \\
0
\end{bmatrix} \text{u}_0(t)
\]

\(\text{u}_0(t) = [0, 0, 0, 1, 1] [i(t), u(t), u_c(t), u_c(t), u_c(t)]^T\)

\[
\frac{\text{d}c(t)}{\text{d}t} = \begin{bmatrix}
0 & -1/L & 0 & 0 & 0 \\
1/C & -1/r+2 & 1/C_r & 1/C_r & -1/C_r & -1/C_r & C_r & C_r & C_r \\
0 & 1/C_r & -1/C_r & -1/C_r & C_r & C_r & C_r & C_r & C_r \\
0 & 1/C_r & -1/C_r & -1/C_r & C_r & C_r & C_r & C_r & C_r \\
0 & 1/C_r & -1/C_r & -1/C_r & C_r & C_r & C_r & C_r & C_r
\end{bmatrix}
\begin{bmatrix}
u_i(t) \\
u_c(t) \\
u_c(t) \\
u_c(t) \\
u_c(t)
\end{bmatrix}
+ \begin{bmatrix}
0 \\
-1/r+2 \\
1/C_r \\
1/C_r \\
1/C_r
\end{bmatrix} \text{u}_0(t)
\]

\(\text{u}_0(t) = [0, 0, 0, 1, 1] [i(t), u(t), u_c(t), u_c(t), u_c(t)]^T\)

\[
\frac{\text{d}i(t)}{\text{d}t} = \begin{bmatrix}
0 & 2d(t)-1/L & 0 & 0 & 0 \\
1-2d(t) & (r+2)(d(t)-1) & 1-d(t) & 1-d(t) & (r+2)(d(t)-1) \\
0 & 1-d(t) & r_d-d(t)(r+2) & r_d-d(t)(r+2) & 0 \\
0 & 1-d(t) & (r+2)(d(t)-1)R_2 & (r+2)(d(t)-1)R_2 & 0 \\
0 & 1-d(t) & (r+2)(d(t)-1)R_3 & (r+2)(d(t)-1)R_3 & 0
\end{bmatrix}
\begin{bmatrix}
u_i(t) \\
u_c(t) \\
u_c(t) \\
u_c(t) \\
u_c(t)
\end{bmatrix}
+ \begin{bmatrix}
0 \\
1-d(t) \\
1-d(t) \\
1-d(t) \\
1-d(t)
\end{bmatrix} \text{u}_0(t)
\]

\(\text{u}_0(t) = [0, 0, 0, 1, 1] [i(t), u(t), u_c(t), u_c(t), u_c(t)]^T\)

\[
\frac{\text{d}c(t)}{\text{d}t} = \begin{bmatrix}
0 & 2D-1/L & 0 & 0 & 0 \\
1-2D & (r+2)(D-1) & 1-D & 1-D & (r+2)(D-1) \\
0 & 1-D & r-2D(r+2) & r-2D(r+2) & 0 \\
0 & 1-D & (D-1)R_2 & (D-1)R_2 & 0 \\
0 & 1-D & (D-1)R_3 & (D-1)R_3 & 0
\end{bmatrix}
\begin{bmatrix}
u_i(t) \\
u_c(t) \\
u_c(t) \\
u_c(t) \\
u_c(t)
\end{bmatrix}
+ \begin{bmatrix}
0 \\
1-D \\
1-D \\
1-D \\
1-D
\end{bmatrix} \text{u}_0(t)
\]

\(\text{u}_0(t) = [0, 0, 0, 1, 1] [i(t), u(t), u_c(t), u_c(t), u_c(t)]^T\)

\[
\frac{\text{d}u(t)}{\text{d}t} = \begin{bmatrix}
0 & 2D-1/L & 0 & 0 & 0 \\
1-2D & (r+2)(D-1) & 1-D & 1-D & (r+2)(D-1) \\
0 & 1-D & r-2D(r+2) & r-2D(r+2) & 0 \\
0 & 1-D & (D-1)R_2 & (D-1)R_2 & 0 \\
0 & 1-D & (D-1)R_3 & (D-1)R_3 & 0
\end{bmatrix}
\begin{bmatrix}
u_i(t) \\
u_c(t) \\
u_c(t) \\
u_c(t) \\
u_c(t)
\end{bmatrix}
+ \begin{bmatrix}
0 \\
1-D \\
1-D \\
1-D \\
1-D
\end{bmatrix} \text{u}_0(t)
\]

\(\text{u}_0(t) = [0, 0, 0, 1, 1] [i(t), u(t), u_c(t), u_c(t), u_c(t)]^T\)
The state-space averaging method is used to model the converter in CCM. \( \text{ut}(t) \) is the input variable, \( \text{vo}(t) \) is the output variable and \( d(t) \) is the control variable. \( \dot{v}(t), u_c(t), u_c(t), u_c(t), u_c(t) \) are the state variables of inductor \( L \) and capacitors \( C_1, C_2, C_3, C_4 \) respectively. When the converter operates in the ON state and the working time is \( dT \), the state space equation is obtained as (21). When the converter operates in the OFF state and the working time is \( (1-d)T \), the state space equation is obtained as (22). In terms of (21) and (22), the state-space averaging equation over a switching period can be obtained as shown in (23). Equation (24) is obtained when all variables are written as the sum of DC and small signals components. By substituting (24) into (23) and removing the DC components, the small signal model of the converter is obtained as shown in (25).

\[
\begin{aligned}
\dot{v}(t) &= I_L + \dot{v}(t) \\
u_c(t) &= U_c1 + \dot{u}_c(t) \\
u_c(t) &= U_c2 + \dot{u}_c(t) \\
u_c(t) &= U_c3 + \dot{u}_c(t) \\
u_c(t) &= U_c4 + \dot{u}_c(t) \\
u_o(t) &= U_o + \dot{u}_o(t) \\
d(t) &= D + \dot{d}(t)
\end{aligned}
\]

where \( I_L, U_{c1}, U_{c2}, U_{c3}, U_{c4}, U_o, D \) are the DC steady-state components of the corresponding variables. \( \dot{v}(t), \dot{u}_c(t), \dot{u}_c(t), \dot{u}_c(t), \dot{u}_c(t), \dot{u}_c(t), \dot{u}_o(t), \dot{d}(t) \) are the small signal components of the corresponding variables.

### Table II

<table>
<thead>
<tr>
<th>Parameters</th>
<th>Values</th>
</tr>
</thead>
<tbody>
<tr>
<td>Rated power ( P )</td>
<td>100 W</td>
</tr>
<tr>
<td>Input voltage ( U_{in} )</td>
<td>25 V-80 V</td>
</tr>
<tr>
<td>Rated output Voltage ( U_o )</td>
<td>200 V</td>
</tr>
<tr>
<td>Rated load resistance ( R_o )</td>
<td>400 ( \Omega )</td>
</tr>
<tr>
<td>Switching frequency ( f )</td>
<td>20 kHz</td>
</tr>
<tr>
<td>Inductor ( L )</td>
<td>800 ( \mu )F</td>
</tr>
<tr>
<td>Capacitors ( C_1, C_2, C_3, C_4 )</td>
<td>470 ( \mu )F</td>
</tr>
<tr>
<td>Power switches ( Q_1, Q_2 )</td>
<td>IXTK102N30P</td>
</tr>
<tr>
<td>Diodes ( D_1, D_2, D_3, D_4 )</td>
<td>DSEC60-03A</td>
</tr>
</tbody>
</table>

The design parameters of the converter are shown in Table II. When \( U_{in}=25 \) V and \( U_o=200 \) V, in terms of (25) and Table II, the transfer functions of control-to-output is obtained as shown in (26).

The dynamic model of proposed converter in (26) is written into the pole-zero form as shown in (27). In order to simplify analysis, the original model in (27) is reduced from 5 to 4 order to obtain the simplified model in (28). By appropriate pole-zero elimination method, the \( (s+3.135 \times 10^5) \) in numerator and the \( (s+4.283 \times 10^5) \) in denominator are eliminated in (27). The BODE diagram curves of (27) and (28) are shown in Figure 7. From Fig. 7, it can be seen that the original and simplified model curves are approximately the same. Therefore, the PI controller is designed based on (28).
\begin{align*}
G_{ZPK}(s) &= \frac{-1.2247 \times 10^9 (s + 3.135 \times 10^5) (s - 1.307 \times 10^5) (s + 3.031 \times 10^5) (s - 0.007247)}{(s + 4.283 \times 10^5)(s + 1.165 \times 10^5)(s + 0.2883)(s^2 + 1.242 \times 10^4 s + 9.04 \times 10^7)} \\
\hat{G}_{ZPK}(s) &= \frac{-1.2247 \times 10^9 (s - 1.307 \times 10^5) (s + 3.031 \times 10^5) (s - 0.007247)}{(s + 1.165 \times 10^5)(s + 0.2883)(s^2 + 1.242 \times 10^4 s + 9.04 \times 10^7)}
\end{align*}

(27)  

\begin{align*}
G_m(s) &= K_F + \frac{K_I}{s} \\
\frac{d(z)}{V_{e}(z)} &= \frac{8 \times 10^{-6} + 7.99 \times 10^{-6} \cdot z^{-1}}{1 - z^{-1}}
\end{align*}

(29)  

(32)

where the \( K_F \) is the proportional coefficient and \( K_I \) is the integral coefficient.

For this work, \( K_F = 0.000008 \) and \( K_I = 0.000005 \). By using PI controller, the Bode diagram of the converter closed-loop system is shown in Fig. 9. The phase margin of the closed-loop system is 53.7°, which indicates the system can achieve stable operation.

\begin{align*}
s &= \frac{2}{T_s} \cdot \frac{z - 1}{z + 1}
\end{align*}

(30)

where \( T_s \) is the sampling period of discrete system. \( T_s = 0.00005s \) in this paper.

In terms of (29) and (30) above, by using bilinear transformation method, the PI controller equation in \( z \) domain is obtained as (31).

\begin{align*}
\frac{d(z)}{V_{e}(z)} &= \frac{(K_F + \frac{T_s}{2} \cdot K_I) \cdot z + \frac{T_s}{2} \cdot K_I - K_F}{z - 1}
\end{align*}

(31)

where \( V_e(z) \) is the input error voltage of PI controller in \( z \) domain. \( d(z) \) is output duty cycle of PI controller in \( z \) domain.

The values of \( K_I, K_F \) and \( T_s \) above are substituted into equation (31) to obtain (32) as follows.

IV. SIMULATION RESULTS AND ANALYSIS

In order to verify the effectiveness of the proposed converter, a simulation model is built for the converter system and simulation parameters are shown in Table II. When the input voltage is \( U_{in} = 25 \) V and the reference output voltage is set as \( U_{O,ref} = 200 \) V, the simulation results are shown in Fig. 10. From Fig. 10, the inductor current \( I_L \) is 7.5 A, which are consistent with the theoretical calculation result in (10). The output voltage \( U_O \) has been stable at 200 V. The voltage stresses across all capacitors and power semiconductors are as follows: \( U_{Q1} = U_{C1} = U_{D1} \approx 75 \) V, \( U_{Q2} = U_{C2} = U_{C3} = U_{D2} = U_{D3} = U_{D4} = U_{D5} \approx 100 \) V, which are consistent with the theoretical calculation results obtained in (8). The simulation results show that the proposed converter has advantages of high-gain and low voltage stresses across components, which verifies the effectiveness of the circuit topology.

The dynamic simulation results of the converter are shown in Figure 11. When the simulation time is 1s, the input voltage of the converter \( U_{in} \) starts to drop from 60V and finally drops to 25V, with a total time of 14s. When the simulation time is 16s, the output current \( I_O \) changes suddenly from 250mA to 500mA and remains 200ms. Then the \( I_O \) changes suddenly from 500mA to 250mA. From Fig. 11, it can be concluded that the converter can maintain the output voltage stable around the reference voltage under the input voltage and load disturbance. The system can obtain a good anti-interference performance.
Fig. 10. Simulation results of converter. (a) Drive voltage $U_{gs}$, inductor current $I_L$, output voltage $U_0$ and voltage stresses across $C_1$, $C_2$, $C_3$, $C_4$. (b) Drive voltage $U_{gs}$, voltage stresses across $Q_1$, $Q_2$, voltage stresses across $D_1$, $D_2$, $D_3$, $D_4$, $D_5$.

V. EXPERIMENTAL RESULTS AND ANALYSIS

The experimental prototype is built based on the circuit topology shown in Fig. 2 to verify the accuracy of theoretical calculation and simulation results. The design parameters of the prototype are shown in Table II. The main controller adopts the TMS320F28335 and the sampling circuits of voltage and current adopt Hall sensors. The experimental prototype is shown in Fig. 12 and the experimental test platform is shown in Fig. 13.

When the input voltage is $U_{in}=25$ V and the reference output voltage is set as $U_{O,ref}=150$ V, the experimental results are shown in Fig. 14. Fig. 14(a) shows the waveforms of drive voltage $U_{gs}$, inductor current $I_L$ and output voltage $U_0$. From Fig. 14(a), it can be seen that the switching frequency of the converter is 20 kHz and the duty cycle is $d=0.4$. When power switches $Q_1$ and $Q_2$ are turned on, inductor $L$ is charged and inductor current $I_L$ increases linearly. When $Q_1$ and $Q_2$ are turned off, inductor $L$ discharges and inductor current $I_L$ decreases linearly. The output voltage $U_0$ of the converter has been stable at the reference value of 150 V. The voltage stresses of all capacitors and power semiconductors are shown in Fig. 14(b)-Fig. 14(e). From these figures, it can be seen that $U_{Q1}=52$
V, $U_{C1}=50$ V and $U_{D1}=50$ V, which are basically consistent with the theoretical calculation result of 50 V obtained in (8). The voltage stresses across other capacitors and power semiconductors are as follows: $U_{Q2}=77$ V, $U_{C2}=72$ V, $U_{C3}=75$ V, $U_{C4}=75$ V, $U_{D2}=75$ V, $U_{Q3}=77$ V and $U_{D3}=75$ V, which are basically consistent with the theoretical calculation result of 75 V obtained in (8).

From Fig. 14, it can be seen from Fig. 15(a) that the switching frequency of the converter is 20 kHz, and the inductor current increases and decreases linearly.

The output voltage $U_O$ of the converter has been stable at the reference value of 200 V. When the closed-loop system is stabilized, the duty cycle of the driving voltage is $d=0.44$, which is slightly higher than the theoretical duty cycle $d=0.428$ obtained in (7). The voltage gain error between actual and the ideal states is caused by the parasitic parameters of the actual components.

When the actual output voltage is less than the reference value, the closed-loop system automatically raises the duty cycle of the driving voltage to increase the output voltage.

From Fig. 15(b)-Fig. 15(e), it can be seen that $U_{Q1}=75$ V, $U_{C1}=72$ V, $U_{D1}=72$ V, which are basically consistent with the theoretical calculation results of 75 V obtained in (8). The voltage stresses across other capacitors and power semiconductors are as follows: $U_{Q2}=100$ V, $U_{C2}=98$ V, $U_{C3}=100$ V, $U_{C4}=100$ V, $U_{D2}=100$ V, $U_{D3}=100$ V and $U_{D4}=99$ V, which are basically consistent with the theoretical calculation results of 100 V obtained in (8).
600 ms. When the input voltage is $U_{in}=25 \, \text{V}$ and the reference output voltage is set as $U_{O_{ref}} = 200 \, \text{V}$, the experimental waveforms during soft-start process are shown in Fig. 18. In (7), the initial voltage gain of converter is already greater than 2 times when duty cycle $\delta$ is approximately 0. Therefore, the output voltage $U_O$, voltages across capacitors and inductor current all have small step changes at the beginning of soft-start in Fig. 18, instead of slowly increasing from zero. Although the small step changes are inevitable, there are no voltage overshoot and impulse current during the whole soft-start process.

Fig. 18. The experimental waveforms of the converter during soft-start process. (a) Output voltage $U_O$. (b) Voltage stresses across $C_1$ and inductor current $I_L$. (c) Voltage stresses across $C_2$, $C_3$, and $C_4$.

The efficiency test experiment is carried out, when the reference output voltage is set as $U_{O_{ref}} = 200 \, \text{V}$ and the input voltage of the converter slowly changes from 30 V to 60 V. The efficiency curves of the prototype are shown Fig. 19. The measured maximum efficiency is 93.1% when the output power is 100 W. When the output power are 80 W and 50 W, the maximum measured efficiencies are 93.8% and 95.4% respectively.

When the output voltage is fixed, the greater the output power, the greater the total loss power. But whether the efficiency is decreasing all the time depends on the increase of the total loss power and the increase of the total output power. In Fig. 19, when $U_{in}=40\, \text{V}$, the total loss power of the $P_{out}=80\, \text{W}$ is 11W and the corresponding efficiency is 87.9%. When $U_{in}=40\, \text{V}$, the total loss power of the $P_{out}=100\, \text{W}$ is 13W and the corresponding efficiency is 88.5%. Although the total loss power of 100W is higher than that of 80W, the increase amplitude of the total loss power is low. Therefore, the efficiency of 100W is slightly higher than that of 80W.

Fig. 17. Output voltage $U_O$ and output current $I_O$ waveforms under load disturbance.

Voltage overshoot and impulse current may occur when the converter is started, which can damage the devices in circuit. In order to avoid the impulse current and voltage during the initial startup instant, a soft-start program is adopted in the controller to make the duty cycle slowly grow from 0 to the desired value. The soft-start time of the experimental prototype is set as 600 ms. When the input voltage is $U_{in}=25 \, \text{V}$ and the reference output voltage is set as $U_{O_{ref}} = 200 \, \text{V}$, the experimental waveforms during soft-start process are shown in Fig. 18. In (7), the initial voltage gain of converter is already greater than 2 times when duty cycle $\delta$ is approximately 0. Therefore, the output voltage $U_O$, voltages across capacitors and inductor current all have small step changes at the beginning of soft-start in Fig. 18, instead of slowly increasing from zero. Although the small step changes are inevitable, there are no voltage overshoot and impulse current during the whole soft-start process.

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VI. CONCLUSION

This paper presents a non-isolated DC-DC converter topology for fuel cell vehicles. The proposed converter can obtain high-gain and wide input voltage range. The voltage gain can reach $2(1-d)/(1-2d)$ and duty cycle $d<0.5$ while achieving high-gain. The voltage stresses across components are less than half of the output voltage, which is beneficial to reduce the size and cost of the converter. In addition, the circuit topology is a common ground structure, which can avoid EMI and safety problems. The converter can always maintain the stability of the output voltage by closed-loop control. There are not the voltage overshoot and impulse current during soft-start process by adopting the soft-start program. Under the rated state, the measured maximum efficiency of the prototype is 93.1%. The proposed converter is suitable for fuel cell vehicles.

REFERENCES


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