Control of Induction Motor Drive using Space Vector PWM

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Abstract—In this paper speed of induction motor is controlled which is fed from three phase bridge inverter. In this paper the speed of an induction motor can be varied by varying input Voltage or frequency or both. Variable voltage and variable frequency for Adjustable Speed Drives (ASD) is invariably obtained from a three-phase Voltage Source Inverter (VSI). Voltage and frequency of inverter can be easily controlled by using PWM techniques, which is a very important aspect in the application of ASDs. A number of PWM techniques are there to obtain variable voltage and variable frequency supply such as PWM, SPWM, SVPWM to name a few, among the various modulation strategies SVPWM is one of the most efficient techniques as it has better performance and output voltage is similar to sinusoidal. In SVPWM the modulation index in linear region will also be high when compared to others.

Keywords—Adjustable Speed Drive (ASD); Voltage source inverter (VSI), Sinusoidal PWM (SPWM), Space Vector PWM (SVPWM).

I. INTRODUCTION

An adjustable speed drive (ASD) is a device used to provide continuous range process speed control. An ASD is capable of adjusting both speed and torque from an induction or synchronous motor. An electric ASD is an electrical system used to control motor speed. ASDs may be referred to by a variety of names, such as variable speed drives, adjustable frequency drives or variable frequency inverters. The two terms adjustable frequency drives or variable frequency inverters will only be used to refer to certain AC systems, as is often the practice, although some DC drives are also based on the principle of adjustable frequency (Switching frequency of chopper switch).

Adjustable speed drives are the most efficient (98% at full load) types of drives. They are used to control the speeds of both AC and DC motors. They include variable frequency/voltage AC motor controllers for squirrel-cage motors, DC motor controllers for DC motors, eddy current clutches for AC motors (less efficient), wound-rotor motor controllers for wound-rotor AC motors (less efficient) and cycloconverters (less efficient).

II. PULSE WIDTH MODULATION (PWM)

Variable voltage and frequency supply for Adjustable Speed Drives (ASD) is invariably obtained from a three-phase VSI. In power electronics, converters and motors, the PWM technique is mostly used to supply AC current to the load by converting the DC current and it appears as an AC signal at load or can control the speed of motors that run at high speed or low. The duty cycle of a PWM signal varies through analog components, a digital microcontroller or PWM integrated circuits.

Figure 1 shows the comparator gets the inputs as reference waveform (square wave) and a carrier wave (triangular wave) is supply to the comparator to obtained PWM waveform. Triangular wave is formed by op-amp driver. Triggering

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pulses are produced at the instant of the carrier signal magnitude is greater than the reference signal magnitude. To turn-on the IGBT switches, firing pulses are produced, the output voltage during the interval triangular voltage wave stipulated the square modulating wave.

**Advantages of PWM technique:**
- Output voltage can be controlled without other components.
- Output voltage can be controlled, lower order harmonics can be eliminated and filtering out higher order harmonics by this filter requirements is minimized.

**Disadvantages of PWM technique:**
- The inverter switches are costly as they must have low turn off and turn on times.

**Types of PWM techniques:**

A number of PWM techniques are there to obtain variable voltage and frequency supply such as,

1. Single-pulse modulation
2. Multiple-pulse modulation
3. Selected harmonic elimination PWM
4. Minimum ripple current PWM
5. Sinusoidal-pulse PWM (SPWM)
6. Space vector-pulse PWM (SVPWM)

**i. Single Pulse Modulation:** The output voltage waveform of single pulse full-bridge inverter is modulated, it contains pulse of width located symmetrically about π/2 and another pulse located symmetrically about 3π/2. The range of pulse width 2d varies from 0 to π; i.e. 0<2d<π. The output voltage is controlled by varying the pulse width 2d. This shape of the output voltage wave is called quasi-square wave.

**ii. Multiple-pulse modulation:** This method of pulse modulation is an extension of single-pulse modulation. In this method, several equidistant pulses per half cycle are used.

**iii. Selected harmonic elimination PWM:**

\[
\sum_{n=1}^{\infty} a_n \cos n \omega t + b_n \sin n \omega t
\]

Where:
\[
a_n = \frac{1}{\pi} \int_0^{2\pi} v(t) \cos n \omega t \, dt; \quad b_n = \frac{1}{\pi} \int_0^{2\pi} v(t) \sin n \omega t \, dt
\]

For a waveform with quarter-cycle symmetry only the odd harmonics with sine components will be present. Therefore, \( an=0 \)

\[
v(t) = \sum_{n=1}^{\infty} (b_n \sin n \omega t)
\]

Where, \( b_n = \frac{4}{\pi} \int_0^{\pi/2} v(t) \sin n \omega t \, dt\)

Assuming that the wave has unit amplitude that is \( v(t)=+1 \), \( bn \) can be expanded and after solving we can get,

\[
v(t) = \sum_{n=1}^{\infty} (-1)^k \sin n \omega t
\]

**iv. Minimum ripple current PWM:** One disadvantage of the SHE PWM method is that the elimination of lower order harmonics considerably boosts the next higher level of harmonics. Since the harmonic loss in a machine is dictated by the RMS ripple current, it is the parameter that should be minimized instead of emphasizing the individual harmonics.

**v. Sinusoidal-pulse PWM (SPWM):** Sinusoidal PWM is a modulation technique in which a sinusoidal signal is compared with the triangular signal, in which the frequency of triangular signal \( f_{tri} \) is equals to the desired sinusoidal output and the frequency of triangular signal gives the switching frequency of the switches.

\[
\frac{\text{ADVANTAGES}}{\text{DISADVANTAGES}} = \frac{\text{amplitude of sinusoidal signal}}{\text{amplitude of triangular signal}}
\]

**ADVANTAGES**
- Controlled inverter output voltage
- Reduction of harmonics

**DISADVANTAGES**
- Increase of switching losses due to high PWM frequency
- Reduction of available voltage
- EMI problems due to high-order harmonics

**Space vector-pulse PWM (SVPWM):** The advance method in PWM techniques is space vector PWM method. It computation intensive PWM method and is excellent method.
among all the PWM techniques for variable frequency drive application. Its characteristic’s is superior to other methods so it is wide spread application in recent years.

III. SPACE VECTOR-PULSE PWM (SVPWM)

It is an algorithm for the control of pulse width modulation (PWM). SVPWM is used for producing of alternating current (AC) waveforms. It is frequently used to drive 3-phase AC powered motors at variable speed from DC power. Various variations of SVPWM that result in different quality and computational requirements. The development is in the reduction of total harmonic distortion (THD) created by the rapid switching inherent to these algorithms.

Space vector modulation is a PWM regulator algorithm for multi-phase AC generation. The reference signal is sampled frequently, after each sample, non-zero active switching vectors adjacent to the reference vector and one or more of the zero switching vectors are preferred for the suitable fraction of the sampling period in order to integrate the reference signal as the average of the used vectors.

Principle of Space Vector PWM:

The circuit model of a typical three-phase voltage source PWM inverter is shown in Fig. 5, S1 to S6 are the six power switches that shape the output, which are controlled by the switching variables \( a, a', b, b', c \) and \( c' \). When an upper IGBT is switched on, i.e., when \( a, b \) or \( c \) is 1, the corresponding lower IGBT is switched off, i.e., the corresponding \( a', b' \) or \( c' \) is 0.

Therefore, the ON and OFF states of the upper IGBTs S1, S3 and S5 can be used to determine the output voltage. The relationship between the switching variable vector and the line-to-line voltage vector is given by in the following:

\[
\begin{bmatrix}
V_{an} \\
V_{bn} \\
V_{cn}
\end{bmatrix} = V_{dc} \begin{bmatrix}
2 & -1 & -1 \\
-1 & 2 & -1 \\
-1 & -1 & 2
\end{bmatrix}
\begin{bmatrix}
a \\
b \\
c
\end{bmatrix}
\]  

(5)

As illustrated in Figure-5, there are eight possible combinations of ON and OFF patterns for the three upper power switches. The on and off states of the lower power devices are opposite to the upper one and so are easily determined once the states of the upper power IGBTs are determined. According to equations (5) and (6), the eight switching vectors, output line to neutral voltage (phase voltage), and output line-to-line voltages in terms of DC link \( V_{dc} \), are given in Table 1, and Fig. 5 shows the eight inverter voltage vectors (V0 to V7).

The major advantage of SVPWM method is from the fact that there is a degree of freedom of space vector placement in a switching cycle. This improves the harmonic performance of this method.

Table 1: Switching vectors, phase voltages and output line to line voltages

![Figure 6: Basic Sector and Vector diagram.](image_url)

To implement the space vector PWM, the voltage equations in the abc reference frame can be transformed into the stationary dq reference frame that consists of the horizontal (d) and vertical (q) axes.
The relation between these two reference frames is below,

\[ f_{dq0} = K_s f_{abc} \]  \hspace{1cm} (7)

\[ K_s = \frac{2}{3} \begin{bmatrix} 1 & -1/2 & -1/2 \\ 0 & \sqrt{3}/2 & -\sqrt{3}/2 \\ 1/2 & 1/2 & 1/2 \end{bmatrix} \]  \hspace{1cm} (8)

\[ f_{dq0} = [f_{dq0}]^T : f_{abc} = [f_{dq0}]^T \]  \hspace{1cm} (9)

And \( f \) denotes either a voltage or a current variable.

As described in Fig. 7, this transformation is equivalent to an
orthogonal projection of \([a,b,c]^T\) onto the two-dimensional
perpendicular to the vector \([1,1,1]^T\) (the equivalent d-q plane)
in a three-dimensional coordinate system. As a result, six non-
zero vectors and two zero vectors are possible. Six nonzero
vectors (V1 - V6) shape the axes of a hexagonal as depicted in
Fig. 7, and feed electric power to the load. The angle between
any adjacent two nonzero vectors is 60 degrees. Meanwhile,
two zero vectors (V0 and V7) are at the origin and apply zero
voltage to the load. The eight vectors are called the basic
space vectors and are denoted by V0, V1, V2, V3, V4, V5,
V6, and V7.

**Steps for implementation of Space vector PWM:**

- **Step 1:** Determine \( V_d, V_q, V_{ref} \) and angle \( (\alpha) \)
- **Step 2:** Determine time duration \( T_1, T_2, T_0 \)

**Step 3:** Determine the switching time of each IGBT (S1 to S6)

**Step 1: Determine \( V_d, V_q, V_{ref} \), and \( (\alpha) \):**

From Fig. 5.5, the \( V_d, V_q, V_{ref} \), and angle \( (\alpha) \) can be
determined as follows:

\[ V_d = v_{an} \frac{1}{2} v_{bn} - \frac{1}{2} v_{cn} \]  \hspace{1cm} (10)

\[ V_q = v_{an} \frac{\sqrt{3}}{2} v_{bn} - \frac{\sqrt{3}}{2} v_{cn} \]  \hspace{1cm} (11)

\[ \begin{bmatrix} V_d \\ V_q \end{bmatrix} = \frac{2}{3} \begin{bmatrix} 1 & -1/2 & -1/2 \\ 0 & 3/2 & -3/2 \end{bmatrix} \begin{bmatrix} v_{an} \\ v_{bn} \\ v_{cn} \end{bmatrix} \]  \hspace{1cm} (12)

\[ |V_{ref}| = \sqrt{v_d^2 + v_q^2}; \alpha = \tan^{-1}\left(\frac{v_q}{v_d}\right) = \omega t = 2\pi ft \]  \hspace{1cm} (13)

Where, \( f \) = fundamental frequency

**Step 2: Determine time duration \( T_1, T_2, T_0 \):**

From Fig. 5.6, the switching time duration can be calculated
as follows:

- **Switching time duration at Sector 1:**

\[ T_0 = T_1 + T_2 + T_0 = T_1 + T_2 \cdot \Psi \]  \hspace{1cm} (14)

\[ T_1 = \frac{\sqrt{3} T_x |V_{ref}|}{V_{dc}} \left( \sin\left(\frac{\pi}{3} - \alpha + \frac{n-1}{3} \pi\right) \right) \]

\[ = \frac{\sqrt{3} T_x |V_{ref}|}{V_{dc}} \left( \sin\left(\frac{n\pi}{3} - \alpha\right) \right) \]  \hspace{1cm} (16)

\[ T_2 = \frac{\sqrt{3} T_x |V_{ref}|}{V_{dc}} \left( \sin\left(\alpha - \frac{n-1}{3} \pi\right) \right) \]

\[ = \frac{\sqrt{3} T_x |V_{ref}|}{V_{dc}} \left( -\cos\alpha \cdot \sin(\frac{n\pi}{3} - \alpha) \cos(\frac{n-1}{3} \pi) \right) \]  \hspace{1cm} (19)

\[ T_0 = T_2 \cdot (T_1 + T_2) \]

Where \( n = 1 \) through 6, \( 0 \leq \alpha \leq 60 \)

**Step 3: Determine the switching time of each IGBT (S1 to S6):**

Following figure gives the switching times of each IGBT
switches. Here Fig. 8 gives the brief idea about the switching
timing pattern of inverter IGBT switches under different
sectors to generate three phase voltage waveform.
Based on above figure, the switching time at each sector is summarized in Table (2), and it will be built in Simulink model to implement SVPWM.

Table 2: Switching time calculation at each sector

<table>
<thead>
<tr>
<th>Sector</th>
<th>Upper Switches (S1,S3,S5)</th>
<th>Lower Switches (S4,S6,S2)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>S1=T1+T2+T0;S3=T1+T0;S5=T0</td>
<td>S1=T0;S3=T1+T0;S5=T1+T2+T0</td>
</tr>
<tr>
<td>2</td>
<td>S1=T1+T0;S3=T1+T2+T0;S5=T0</td>
<td>S1=T2+T0;S3=T2;S5=T1+T2+T0</td>
</tr>
<tr>
<td>3</td>
<td>S1=T0;S3=T1+T2+T0;S5=T2+T0</td>
<td>S1=T1+T2+T0;S3=T0;S5=T1+T0</td>
</tr>
<tr>
<td>4</td>
<td>S1=T0;S3=T1+T0;S5=T1+T2+T0</td>
<td>S1=T1+T2+T0;S3=T2;S5=T0</td>
</tr>
<tr>
<td>5</td>
<td>S1=T1+T2+T0;S3=T0;S5=T1+T2+T0</td>
<td>S1=T0;S3=T1+T2+T0;S5=T2+T0</td>
</tr>
<tr>
<td>6</td>
<td>S1=T1+T2+T0;S3=T0;S5=T1+T2+T0</td>
<td>S1=T0;S3=T1+T2+T0;S5=T2+T0</td>
</tr>
</tbody>
</table>

IV. SIMULATIONS AND RESULTS

Simulation of sinusoidal PWM based model:

In Sinusoidal PWM three phase reference modulating signals are compared against a common triangular carrier to generate the PWM signals for the three phases. It is simple and linear between 0% and 78.5% of six step voltage values, which results in poor voltage utilization. Frequency in conventional SPWM output waves owing to their fixed switching frequencies.

The simulation circuit connection of a three phase inverter based induction motor drive with Sinusoidal PWM (SPWM) is as shown in above figure. Here the three-phase 415V, 50Hz ac supply is converted into dc and then this DC voltage is converted into 3-phase variable frequency ac. Here the controlling of inverter is done by PWM method i.e. sinusoidal PWM.

The speed and electromagnetic responses of induction motor with the different load torques at different instants are as shown in Fig. 11. From this figure it is observed that when load is applied on the motor the speed of motor gets reduced.
Simulation of Space Vector PWM based model:

i) Open Loop Model:

SVPWM based pulse generator simulation diagram is as shown in Fig. 14. The switching times of switches T1, T3 and T5 are determined in the block MATLAB function block to which some parameters are given such as sector number, angle (α), Vref and sampling time. The switching times T1, T3 and T5 are calculated in 6 sectors individually by changing the sector. The output of the block is T1, T3 and T5 which is again compared with the high frequency carrier wave so as to reduce the harmonics in the output of inverter. And T4, T6 and T2 are the inverted switching times of T1, T3 and T5 respectively.

T1 to T6 pulse signals are as shown in Fig. 12. These pulsed are given to the six IGBT switches of bridge inverter.

Figure 11: Motor Speed and Electromagnetic torque.

Figure 12: SVPWM output gate pulses

When SVPWM pulse generator is connected to 3-phase bridge inverter with the induction motor load form a open loop drive. The motor will run at a reference speed. The reference speed command is converted into frequency command and given to SVPWM block. The SVPWM block generates gate pulses with respect to speed command so as to run motor at reference speed.

The reference speed and motor speed graph with time and load torque=0 are as shown in below figure.
Figure 14: Open Loop Drive Speed response with different TL

Figure 15: SPWM based open loop drive Load Current THD

Table 3, variation of motor speed and load current response in gives the open loop model with different load torque. Also table 4, shows closed loop response with different load torques.

**Table (3): Open Loop Model Variation of motor speed with Load torque**

<table>
<thead>
<tr>
<th>S. No.</th>
<th>Load Torque TL (N-m)</th>
<th>Speed (rpm) SVPWM</th>
<th>Load Current (Amps)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1.</td>
<td>0</td>
<td>1391</td>
<td>1.5</td>
</tr>
<tr>
<td>2.</td>
<td>5</td>
<td>1374</td>
<td>2.1</td>
</tr>
<tr>
<td>3.</td>
<td>9</td>
<td>1359</td>
<td>5.3</td>
</tr>
<tr>
<td>4.</td>
<td>11</td>
<td>1352</td>
<td>6.4</td>
</tr>
</tbody>
</table>

**Table (4): Open Loop Model Variation of motor speed with Load torque**

<table>
<thead>
<tr>
<th>S. No.</th>
<th>Load Torque (N-m)</th>
<th>Speed (rpm) SVPWM</th>
<th>Load Current (Amps)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1.</td>
<td>0</td>
<td>1390</td>
<td>1.4</td>
</tr>
<tr>
<td>2.</td>
<td>5</td>
<td>1375</td>
<td>1.9</td>
</tr>
<tr>
<td>3.</td>
<td>9</td>
<td>1362</td>
<td>5.2</td>
</tr>
<tr>
<td>4.</td>
<td>11</td>
<td>1354</td>
<td>6.4</td>
</tr>
</tbody>
</table>

To maintain the motor speed at a reference speed value, it needs a feedback loop of motor speed and a speed controller. The drive requires a speed sensor, and the output of the speed sensor will be in terms of rpm. This speed will be processed in the speed controller as explained in the above session.

**V. CONCLUSION**

The simulation of “Control of Induction Motor Drive Using Space Vector PWM” is carried out in MATLAB/Simulink. The simulation has been done for open loop as well as closed control. The appropriate output results are obtained. The variation of speed of Induction Motor has been observed by varying the load torque in open loop control and results are noted down in the table. Also observed that for the change in input speed commands the motor speed is settled down to its final value within 0.1sec in closed loop model.

**REFERENCES:**


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